

HW #2 p. 9-10 #1-13 odd, 31, 35, 39, 41, 49, 54-57, 59, 81

Set Builder

Interval Notation

1.  $x > 50$   $\{x \mid x > 50, x \in \mathbb{R}\}$   $(50, \infty)$
3.  $x \leq -4$   $\{x \mid x \leq -4, x \in \mathbb{R}\}$   $(-\infty, -4]$
5.  $8 < x < 99$   $\{x \mid 8 < x < 99, x \in \mathbb{R}\}$   $(8, 99)$
7.  $x < -19$  or  $x > 21$   $\{x \mid x < -19 \text{ or } x > 21, x \in \mathbb{R}\}$   $(-\infty, -19) \cup (21, \infty)$
9.  $\{-0.25, 0, 0.25, 0.50, \dots\}$   $\{x \mid x = 0.25n, n \geq -1, n \in \mathbb{Z}\}$  N/A
11.  $x \leq -45$  or  $x > 86$   $\{x \mid x \leq -45 \text{ or } x > 86, x \in \mathbb{R}\}$   $(-\infty, -45) \cup (86, \infty)$
13. all multiples of 5  $\{x \mid x = 5n, n \in \mathbb{Z}\}$  N/A
31.  $h(y) = -3y^3 - 6y + 9$
- a.  $h(4) = -3(4)^3 - 6(4) + 9$   
 $= -3(64) - 24 + 9$   
 $= -192 - 24 + 9 = -207$
- b.  $h(-2y) = -3(-2y)^3 - 6(-2y) + 9$   
 $= -3(-8y^3) + 12y + 9$   
 $= 24y^3 + 12y + 9$
- c.  $h(5b+3) = -3(5b+3)^3 - 6(5b+3) + 9$

$$= -3(5b+3)^2(5b+3) - 30b - 18 + 9$$

$$= -3(25b^2 + 30b + 9)(5b+3) - 30b - 9$$

$$= -3(125b^3 + 150b^2 + 45b + 75b^2 + 90b + 27) - 30b - 9$$

$$= -3(125b^3 + 225b^2 + 135b + 27) - 30b - 9$$

$$= -375b^3 - 675b^2 - 405b - 81 - 30b - 9$$

$$= \underline{-375b^3 - 675b^2 - 435b - 90}$$

35.  $f(x) = -7 + \frac{6x+1}{x}$

a.  $f(5) = -7 + \frac{6(5)+1}{5}$   
 $= -7 + \frac{30+1}{5}$   
 $= -7 + \frac{31}{5}$

$\rightarrow \frac{-35}{5} + \frac{31}{5}$   
 $= \left(-\frac{4}{5}\right)$  or  $(-0.8)$

b.  $f(-8x) = -7 + \frac{6(-8x)+1}{-8x}$   
 $= -7 + \frac{-48x+1}{-8x}$   
 $= -7 + \frac{-48x}{-8x} + \frac{1}{-8x}$

$\rightarrow = -7 + 6 - \frac{1}{8x}$   
 $= \left(-1 - \frac{1}{8x}\right)$

c.  $f(6y+4) = -7 + \frac{6(6y+4)+1}{6y+4}$   
 $= -7 + \frac{36y+24+1}{6y+4}$

$\rightarrow = -7 + \frac{36y+25}{6y+4}$

$$39. f(x) = \frac{8x+12}{x^2+5x+4} \rightarrow (x+4)(x+1) = 0$$

$$x \neq -4 \quad x \neq -1$$

$$\{x \mid x \neq -4, x \neq -1, x \in \mathbb{R}\} \text{ or } (-\infty, -4) \cup (-4, -1) \cup (-1, \infty)$$

$$41. g(a) = \sqrt{1+a^2} \quad (-\infty, \infty)$$



$$49. f(-5) = (-5)^2 + (-5) + 1 = 25 - 5 + 1 = 21$$

$$f(12) = (12)^2 + 12 + 1 = 144 + 12 + 1 = 157$$

54. yes, a vertical line only passes through each point once.

55. no, a vertical line would pass through the inequality infinitely many points.

56. yes, a vertical line only passes through each point once.

57. no, a vertical line would pass through twice at  $(0, 0)$  and  $(0, -4)$ .

59. Since the president is elected every 4 years it would not make sense to use interval notation. Elections began in 1792 so set builder notation:  $\{x \mid x = 4n + 1792, n \in \mathbb{W}\}$

$$81. f(x) = \frac{1}{(x+3)(x+1)(x-5)} \quad (x+3)(x+1)(x-5) = 0$$
$$x \neq -3, -1, 5$$

Interval Notation

$$(-\infty, -3) \cup (-3, -1) \cup (-1, 5) \cup (5, \infty)$$

Set Builder

$$\{x \mid x \neq -3, x \neq -1, x \neq 5, x \in \mathbb{R}\}$$

I prefer set builder because instead of listing 4 intervals you can list the values  $x$  can't equal.